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**3(Sem-8/FYUGP)BNC(A)/DSCI**

**2025**

**STATISTICS**

*(Discipline Specific Core)*

**Paper Name: Statistical Inference-2**

Paper Code: **STA-DSC-244**

*Full Marks: 45*

*Time: Two Hours*

*(The figures in the margin indicate full marks for the questions)*

1. **Answer the following questions:** **1x4=4**
  - a) Critical region is also known as----- . **(Fill in the blank)**
  - b) Define type – I error.
  - c) State any one property of likelihood ratio test.
  - d) Non-parametric test does not make any assumption regarding the form of population. **(State true or false)**
  
2. **Answer any three of the following questions:** **2x3=6**
  - a) Define simple and composite hypothesis with example.
  - b) What are the properties of good estimator?
  - c) Write the advantages of non-parametric methods over parametric methods.
  - d) Define Uniformly Most Powerful (UMP) test.
  
3. **Answer any three of the following questions:** **5x3=15**
  - a) Differentiate between null and alternative hypothesis with an example.

- b) State and prove Neyman Pearson lemma.
- c) Describe briefly the method of moments for estimation.
- d) Write a note on Kolmogorov-Smirnov test for one sample.
- e) State and prove the invariance property of consistent estimator.

**4. Answer any two of the following questions: 10x2=20**

- a) Explain the likelihood ratio test. Let  $x_1, x_2, x_3, \dots, x_n$  be a random sample from  $N(\mu, \sigma^2)$ , where  $\sigma^2$  is known. Develop likelihood ratio test for  $H_0: \mu = \mu_0$  against  $H_1: \mu > \mu_0$ . 4+6=10
- b) State and prove Cramer-Rao inequality. Also mention the regularity conditions involved. 2+5+3=10
- c) (i) Define a run. Mention the certain assumptions associated with non-parametric test. 2+3=5  
(ii) Write a note on sign test for sample. 5

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