4. (a) Estimate the parameters of the linear model  $Y = \alpha + \beta X + U$ . Show that  $E(\hat{\alpha}) = \alpha$ ,  $E(\hat{\beta}) = \beta$  where  $\hat{\alpha}$  and  $\hat{\beta}$  are least square estimators for  $\alpha$  and  $\beta$ . Also find standard errors of  $\hat{\alpha}$  and  $\hat{\beta}$ . 3+3+4=10

## Or

- (b) State and prove Gauss-Markov theorem. 10
- 5. (a) Discuss the properties of least square estimators.

## Or

- (b) Discuss the limitations of econometrics. Also describe the methodology involved in an econometric model. 5+5=10
- 6. (a) Write short notes on: 5×2=10
  (i) Multicollinearity
  (ii) Heteroscedasticity

## Or

(b) Write a note on hypothesis testing. Explain how you would construct 95% confidence intervals for the parameters  $\alpha$  and  $\beta$  in the simple linear model  $Y = \alpha + \beta X + U$ . 4+3+3=10

Total number of printed pages-4

3 (Sem-6/CBCS) STA HE 1

2023

## STATISTICS

(Honours Elective)

Paper: STA-HE-6016

(Econometrics)

Full Marks: 60

Time: Three hours

The figures in the margin indicate full marks for the questions.

- 1. Answer the following questions as directed:  $1 \times 7 = 7$ 
  - (a) The regression model is linear in the parameters. (Write True or False)
  - (b) If  $E(U_iU_j)=0$  for  $i \neq j \ \forall i, j$  in the linear model  $Y_i=\alpha+\beta X_i+U_i$ , then the disturbance values are known as \_\_\_\_\_. (Fill in the blank)

- (c) What do you understand by BLUE?
- (d) Homoscedasticity refers to the error terms having
  - (i) zero mean
  - (ii) positive variance
  - (iii) constant variance
  - (iv) positive mean
    (Choose the correct option)
- (e) Data collected at a point in time is called \_\_\_\_\_. (Fill in the blank)
- (f) In  $Y_i = \hat{\beta}_1 + \hat{\beta}_2 X_i + \hat{U}_i$ ,  $\hat{U}_i$  gives the differences between
  - (i) the actual and estimated Y values
  - (ii) the actual and estimated X values
  - (iii) the actual and estimated beta values
  - (iv) the actual and estimated U values (Choose the correct option)

(Write True or False)

(g) For coefficient of determination  $r^2$  for a regression model  $0 \le r^2 \le 1$ .

2. Answer the following questions: 2×4=8

- (a) What do you understand by 'econometrics'?
- (b) Define time series data.
- (c) Write the objectives of econometrics.
- (d) What is the significance of  $b_{yx}$  the regression coefficient of Y on X?
- 3. Answer **any three** from the following questions: 5×3=15
  - (a) Write a note on coefficient of determination  $r^2$ .
  - (b) Write the assumptions in the three variable regression model  $Y_i = \beta_1 + \beta_2 X_{2i} + \beta_3 X_{3i} + U_i.$
  - (c) Write a note on the scope of econometrics.
  - (d) Discuss the linear model used in econometrics.
  - (e) Write a note on autocorrelation.